

CS m51A: Logic Design of Digital Systems
UCLA Computer Science Department
Winter 2010
Midterm 2

Time: 100 minutes

Note: Closed book, closed notes, no electronic computing or communications devices.

Name: _____

Student ID: _____

Solutions

Question	Points	Grades
1	20	
2	20	
3	15	
4	20	
5	25	
Total	100	

"The process of preparing programs for a digital computer is especially attractive, not only because it can be economically and scientifically rewarding, but also because it can be an aesthetic experience much like composing poetry or music."

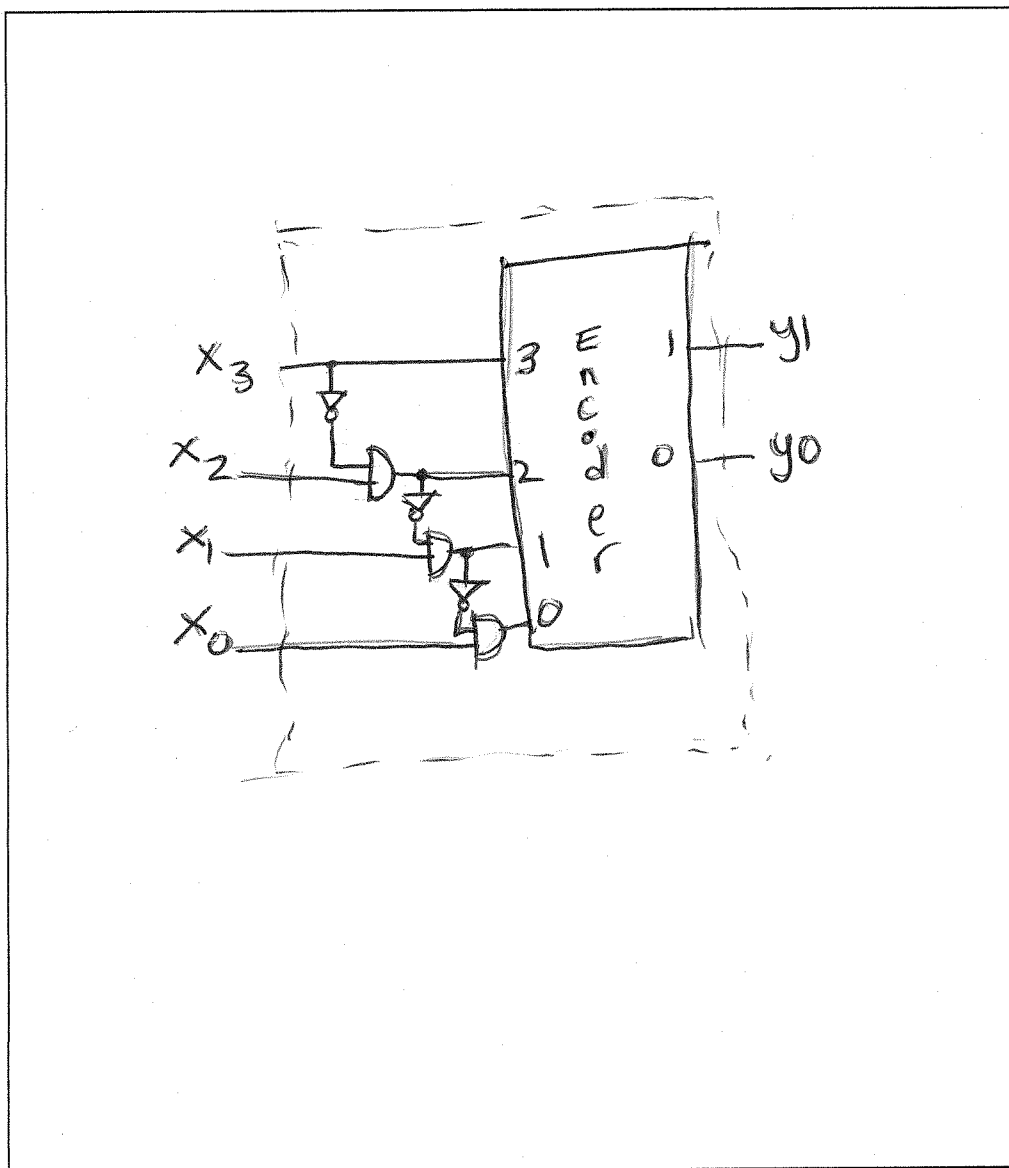
- Donald E. Knuth

Question 1: Priority Encoder

Design a 4-bit priority encoder, where a priority encoder converts a 4-bit input into a binary representation of the signal with the highest priority. The table below summarizes the functionality.

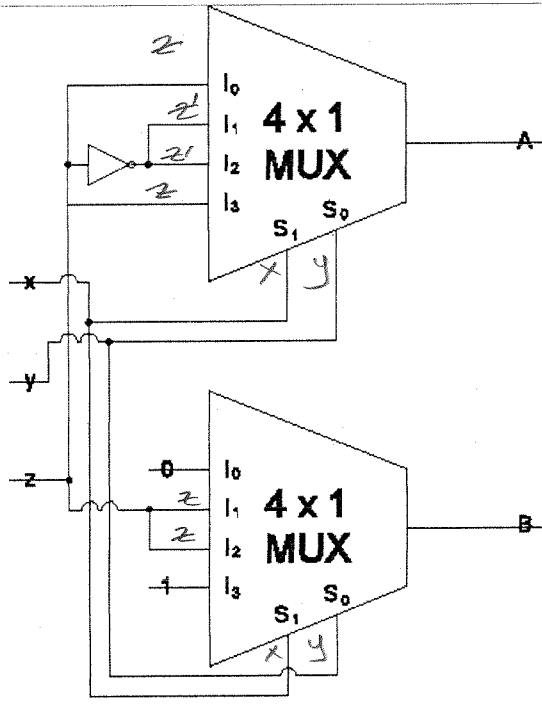
Input	Output
x_3, x_2, x_1, x_0	y_1, y_0
1---	11
01--	10
001-	01
000-	00

For full credit use an encoder and the minimum number of gates.



Question 2:

- a) Give switching functions to describe the functionality of the outputs A and B, in the following circuit. For credit, show your work.



$$A = x'y'z + x'yz' + xy'z' + xyz$$

$$B = xy + x'yz + xy'z$$

Use a truth table to help figure out part b.

x	y	z	B	A
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

- b) The circuit shown in a) has the functionality of a commonly used arithmetic component. What does the circuit do and what are other names for A and B?

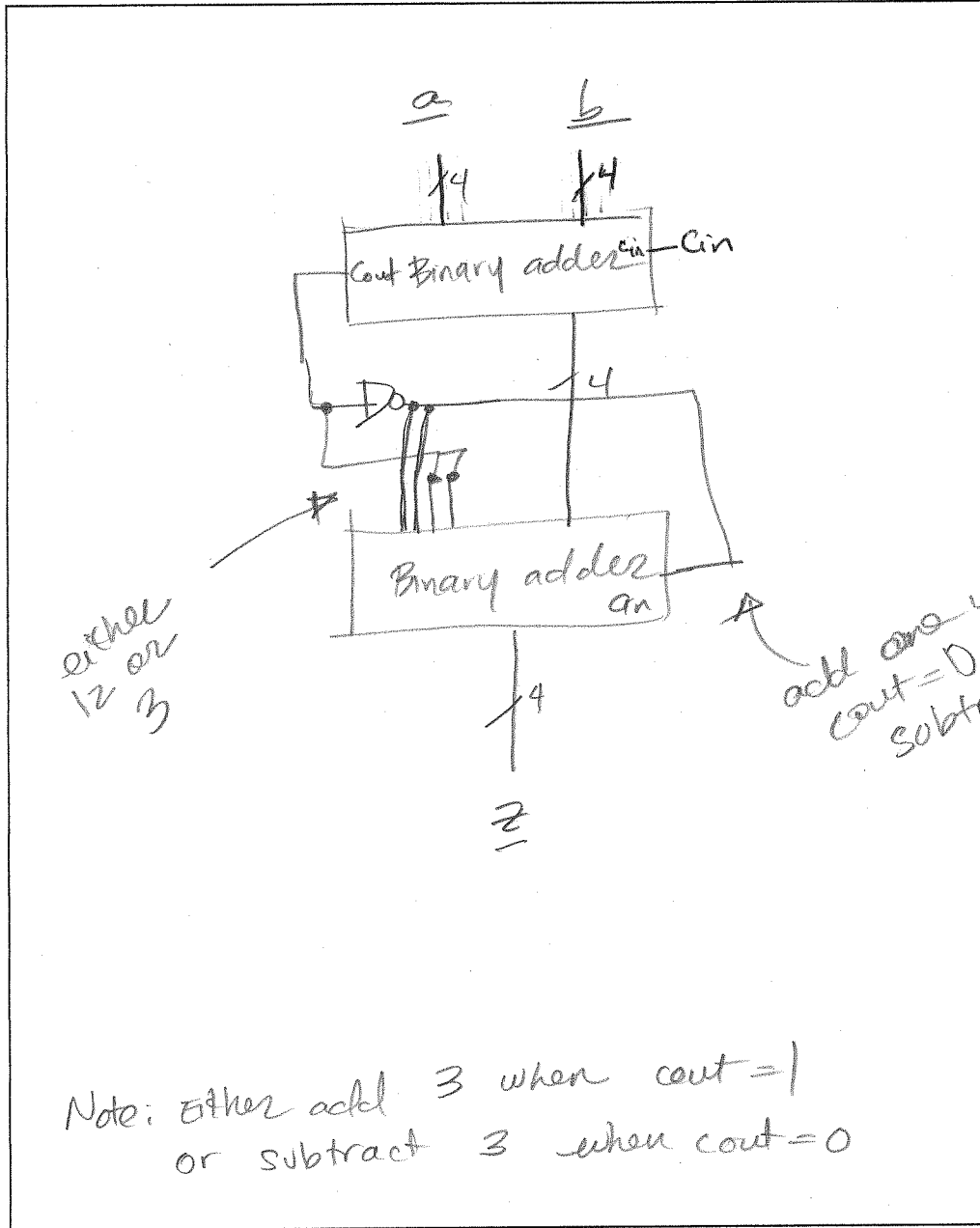
$$A = \text{sum of } x+y+z$$

$$B = \text{carry out of } x+y+z$$

→ adder.

Question 3: Excess-3 Addition

Design a one-digit decimal adder in the Excess-3 code, which takes as input two Excess-3 coded digits, \underline{a} and \underline{b} and outputs an Excess-3 coded digit, \underline{s} , and a one-bit carry-out bit. For example, the inputs $\underline{a} = 0111$ and $\underline{b} = 1011$, would produce the output $\text{cout} = 1$ and $\underline{s} = 0101$. Use two four-bit binary adders and one inverter, for full credit.



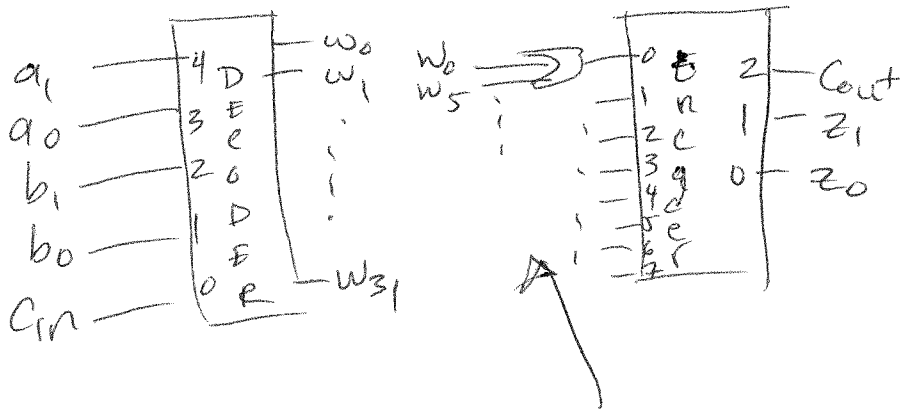
Question 4: One's Complement Addition

Implement a 2-bit one's complement adder using only an encoder, a decoder, and a minimal number of gates. For full credit, show your work. Make sure to consider the carry-in and the carry-out bits.

Step 1: Create Truth table

$a_1 a_0 b_1 b_0 C_{in}$	$C_{out} z_1 z_0$
00000	0 0 0
00001	0 0 1
00010	0 0 1
1	1
1	1

Step 2: Figure out mapping from decoder to encoder



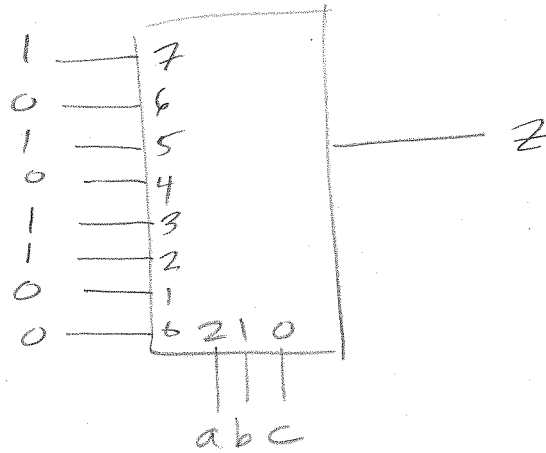
Have one OR Gate for each input to the Encoder

or the outputs of the decoder appropriately

Question 4:

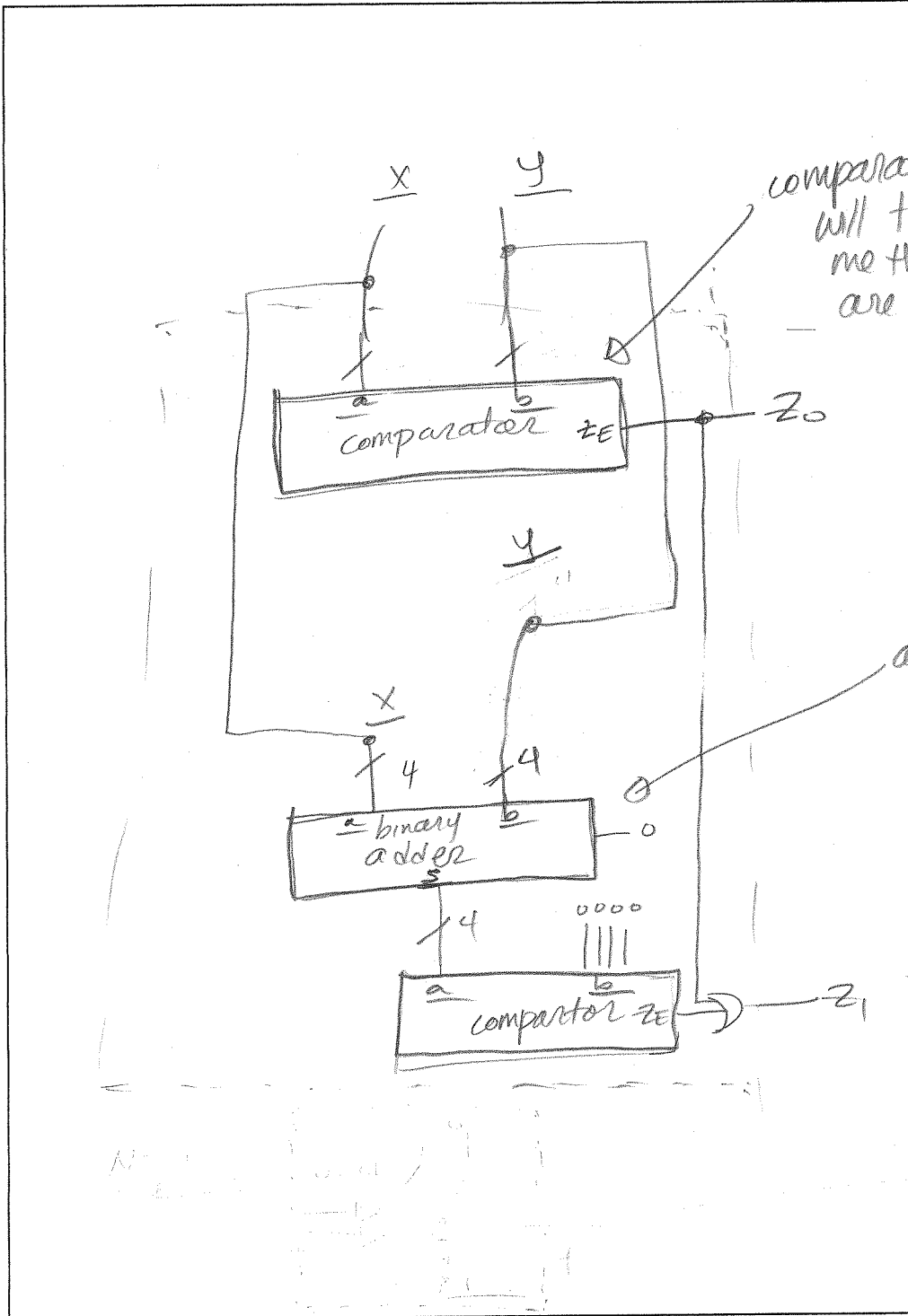
Design a 3-bit prime number detector (PND). PND gets a three digit binary number, $n=(a,b,c)$, and outputs 1 if n is prime. Design this module using only one 8-1 multiplexer with no additional logic. Note: 0 and 1 are not prime numbers.

0, 1, 4, 6 - not prime numbers
2, 3, 5, 7 - prime numbers



Question 5:

Using standard modules and a minimum number of gates, design a combinational system that given two's complement 4-bit inputs, \underline{x} and \underline{y} , outputs $z_0=1$ when $\underline{x} = \underline{y}$, and $z_1=1$ when $|\underline{x}| = |\underline{y}|$. Make sure to define user-defined modules when appropriate.



comparator will tell me they are equal

$$\begin{aligned} x &= x \\ -x &= -x \end{aligned}$$

adding two numbers which are the negation of each other will give a sum = 0.

$$x - x = 0$$

$$x + x = 0$$