Sparse PCA corrects for cell type heterogeneity in epigenome-wide association studies

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In epigenome-wide association studies (EWAS), different methylation profiles of distinct cell types may lead to false discoveries. We introduce ReFACTor, a method based on principal component analysis (PCA) and designed for the correction of cell type heterogeneity in EWAS. ReFACTor does not require knowledge of cell counts, and it provides improved estimates of cell type composition, resulting in improved power and control for false positives in EWAS. Corresponding software is available at http://www.cs.tau.ac.il/~heran/ cozygene/software/refactor.html.

Recent work applying EWAS suggests an important role for DNA methylation as a mechanism involved in disease. In a standard EWAS of primary tissue, such as whole blood, methylation data represent the epigenetic states of a heterogeneous mixture of cell types. Since the epigenome is highly variable across different cell types, correlations between the phenotype of interest and the cell type composition lead to a large number of false discoveries^{1,2}.

The standard statistical analysis applied in EWAS uses a univariate test for correlation between the phenotype and each of the probed CpG sites. Thus, false discoveries due to cell type heterogeneity can be addressed by adding the cell proportions as covariates. However, cell type compositions are not typically measured, and therefore a computational method has been proposed for the estimation of cell type composition using a reference data set that includes methylation measurements for sorted cells³. Unfortunately, reference data for whole-genome methylation levels from sorted cells are available only for a small subset of different blood cells and not for any other tissues. Furthermore, the existing data sets are small^{3,4}, and the individuals in the reference data are not matched for methylation-altering factors such as age and sex, which may lead to inaccuracies in the cell type estimates. As a result of the above limitations, reference-free methods, which do not rely on external reference data, have been proposed^{2,5}.

We show that none of the current methods adequately controls for false positives, and we present a new method, reference-free adjustment for cell type composition (ReFACTor), to address the shortcomings of current methods. ReFACTor is based on a variant of PCA and can be applied to any tissue. PCA is a natural candidate for the correction of cell type heterogeneity, since the first several principal components (PCs) are correlated with cell type composition⁶. However, only a small number of sites (known as differentially methylated regions, or DMRs) differ significantly between cell types, and therefore using all the sites in PCA potentially reduces the correlation. Motivated by this observation, we designed ReFACTor to perform a PCA on a subset of the sites that are differentially methylated across the different cell types rather than on the entire set of CpG methylation sites. Specifically, ReFACTor selects the sites that can be reconstructed with low error using a low-rank approximation of the original methylation matrix. In contrast to other methods in which unsupervised site selection is performed based on the correlation between the site and the phenotype, ReFACTor does not use the phenotype in the selection process, making ReFACTor useful as part of a quality control step in EWAS.

We evaluated the ability of ReFACTor to capture cell type composition using simulations and real data. We first simulated mixture of cell types and measured the correlation of the PCs of ReFACTor (ReFACTor components) with the cell proportions. We observed that the correlation between each of the cell types and the linear predictor of the cell type using the first several ReFACTor components was substantially improved compared with the correlation using the first several PCs of a standard PCA. These results were robust to the simulation parameters (see Online Methods and Supplementary Figs. 1-3).

Next, we measured the performance of ReFACTor on real data from the GALA II data set⁷ (n = 489). The GALA II cohort contains whole blood methylation data as well as cell count measurements for 78 of the samples, and so we were able to evaluate the correlation between the measured cell type proportions and the inferred ReFACTor components. We compared the results of ReFACTor to PCA and to the available reference-based method³ (Fig. 1). Overall, ReFACTor's correlation with the cell type proportions is higher than PCA's, and ReFACTor outperforms the reference-based method with six components—six being the number of cell types it estimates—even though the referencebased method leverages external data not available to ReFACTor. Although cell counts could potentially be used to adjust for tissue

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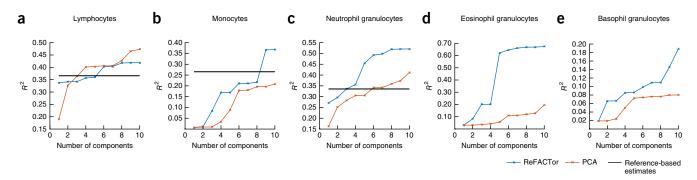


Figure 1 | The fraction of variance explained in each of the cell types for which cell counts were available in the GALA II data set (78 samples). The ReFACTor components are in blue, the PCs of standard PCA are in red, and the available estimates of the reference-based method are in black. (a-e) Shown are correlations with (a) lymphocyte cell count as a function of the number of components used in the linear predictor (squared linear correlation), (b) monocyte cell count, (c) neutrophil granulocyte cell count, (d) eosinophil granulocyte cell count, and (e) basophil granulocyte cell count.

heterogeneity in EWAS, we observed that false discoveries can arise in the common case where cell counts are measured or estimated only for a small number of preselected cell types (see **Supplementary Note**). False discoveries arise particularly in the absence of cell counts for cell types that are correlated with the phenotype. In contrast, we found that ReFACTor's PCs provide a good correction in such settings (Supplementary Tables 1 and 2 and Supplementary Figs. 4 and 5).

We further evaluated the control for false positives of ReFACTor using simulations. For each simulated data set we generated a phenotype using a linear model of the cell type proportions and a randomly chosen causal methylation site (Online Methods). We compared five approaches for EWAS analysis: uncorrected linear regression, linear regression with PCA, linear regression using ReFACTor components, FaST-LMM-EWASher², and RefFreeEWAS⁵. We found that none of these methods adequately controls for false positives; however, ReFACTor obtains a significantly reduced level of false discoveries (Supplementary Fig. 6).

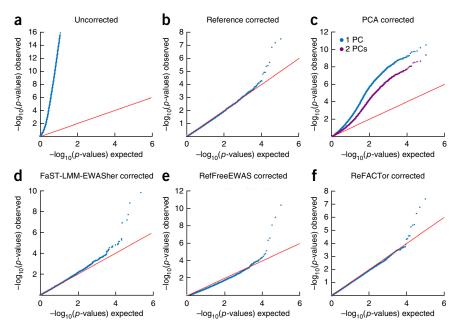
We compared the fraction of simulated data sets in which the truly associated methylation site obtained the best P value (the

detection power). We observed that the detection power was significantly higher using ReFACTor compared with other methods (Supplementary Fig. 7). We further considered the scenario in which the methylation differences in the causal site between the various levels of the phenotype are cell specific and the scenario in which multiple sites are causal (Online

Figure 2 | Results of the RA methylation analysis, presented by quantile-quantile plots of the $-\log_{10} P$ values for the association tests. Significant deviation from the red line indicates an inflation arising from a confounder in the data. (a-e) Shown are (a) No correction, (b) correction using the reference-based estimates of the cell type proportions, (c) correction using the first couple of PCs of a standard PCA, (d) correction using FaST-LMM-EWASher, (e) correction using RefFreeEWAS and (f) correction using the first ReFACTor component.

Methods). In both scenarios, ReFACTor outperforms all other methods (Supplementary Figs. 8 and 9).

The correlation between the cell type composition and ReFACTor's PCs potentially allows for an improved correction of EWAS. We performed an EWAS using whole blood methylation data from a recent study with rheumatoid arthritis (RA)8. Since the cell composition of blood in RA patients typically differs from that in the general population⁹, there is a risk for false discoveries that stem from unaccounted-for cell type heterogeneity. We performed different approaches for the correction of false discoveries (Fig. 2). As a baseline, we performed a logistic regression without adjusting the data for cell composition, which resulted in a severe inflation of the test statistic that was consistent with the results reported in previous studies^{2,5,8}. We then adjusted the data using the estimates of the cell type proportions obtained by the reference-based method³. This correction removed the inflation by eliminating the cell composition confounder. We then proceeded with unsupervised methods for cell type correction, using the first several PCs of a standard PCA, FaST-LMM-EWASher², and RefFreeEWAS⁵. None of these unsupervised approaches allowed us to reconstruct the results obtained using the reference-based



approach. In contrast, adjusting the data with only one ReFACTor component eliminated the inflation and revealed the three significant associations that were found by the reference-based approach (Supplementary Table 3).

We observed that both ReFACTor and the reference-based method resulted in a small number of significant sites in comparison with the uncorrected analysis. Theoretically, both of these methods might have overcorrected true signals. In order to exclude this possibility, we repeated the analysis using a set of sites chosen for the PCA step of ReFACTor that were selected by considering only the controls and discarding the cases. This procedure also resulted in the same three associated sites (Supplementary Fig. 10). Since the PCA was performed on a small number of sites that were selected using a group of healthy samples, an overcorrection was not likely in this case.

Similar to PCA, ReFACTor allows for the flexibility to efficiently perform any desired downstream analysis once regressing out the ReFACTor components. Two such desired analyses include association testing for a large number of phenotypes and logistic regression for dichotomous phenotypes. In addition, regressing out the ReFACTor components makes it possible to run permutation tests efficiently, since the permutation needs to be performed on the residuals of the methylation data. We note that, in principle, modifications of other existing methods^{2,5} could lead to similar utility in those methods.

The underlying assumption of ReFACTor is that the confounders are affected by a sparse set of methylation sites. Future work may further improve the performance of ReFACTor by using other feature-selection algorithms and by optimizing the selection of the dimension parameters used in the algorithm.

Although our experiments focused on cell type composition, we believe that ReFACTor is likely to perform well on other unknown confounders in EWAS. Other known confounders such as sex and age are also affected by a sparse set of CpGs^{10,11}. However, as for any other unsupervised method, it is important to consider the possibility that an unknown confounder was not captured by the method because of deviations from the assumptions. Moreover, since ReFACTor corrects principal components of a set of DMRs, if by chance many of these DMRs are causal, ReFACTor will result in overcorrection and loss of power. Our suggested approach, in which the DMRs are chosen based on the controls alone, should alleviate this potential risk.

METHODS

Methods and any associated references are available in the online version of the paper.

Accession codes. The GALA II methylation data are now publicly available in the Gene Expression Omnibus (GEO) database (accession number GSE77716). The RA data are publicly available and were downloaded from the GEO database (accession number GSE42861). Methylation levels of sorted white blood cells for the simulations were downloaded from the GEO database (accession number GSE35069).

Note: Any Supplementary Information and Source Data files are available in the online version of the paper.

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AUTHOR CONTRIBUTIONS

E.R. and E.H. designed research, performed research, contributed analytic tools, analyzed data and wrote the paper. N.Z. and E.E. helped with experimental design, data interpretation, and drafting of the paper. Y.B. and J.Z. contributed expertise. C.E., D.H., J.G., S.O. and E.G.B. generated and contributed the data. D.H. also performed quality control analysis.

COMPETING FINANCIAL INTERESTS

The authors declare no competing financial interests.

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ONLINE METHODS

The ReFACTor algorithm. We assume that methylation levels have been measured at m methylation sites across n individuals. Let O_i be an $m \times 1$ vector of observed beta-normalized methylation levels in an individual i, and let R_i be a $k \times 1$ vector corresponding to the individual's specific cell type composition. That is, R_{hi} is the fraction of cell type h in individual i. Furthermore, let M be an $m \times k$ matrix corresponding to the mean value of each site for each cell type, i.e., M_{jh} is the mean methylation value of cell type h at CpG site j. The following generative model motivates the approach taken in ReFACTor. We assume the methylation level at site j cell type h to be normally distributed with mean M_{jh} and that the methylation measurement error is also normally distributed with mean 0. Thus, the model we assume can now be summarized as

$$O_i = MR_i + \varepsilon_i$$

where ε_i is normally distributed. Effects known to be correlated with methylation (for example, age¹⁰, sex¹¹, smoking¹², and DNA sequence variation^{13,14}) can be added to the model as fixed linear effects and can be regressed out.

The ReFACTor algorithm gets, as an input, an observed $m \times n$ methylation matrix O, the number of assumed cell types k in the data, and the number of DMRs t. After the centering and standardization of each site, the goal of the algorithm is to find an \hat{R} that is correlated with the real cell type proportions R. The algorithm proceeds as follows.

- Find a matrix V of dimensions m × k, consisting of the top k left-singular vectors of O (i.e., the top k eigenvectors of OO^t).
- (2) Compute $\tilde{O} = VV^tO$, which is the *k*-rank approximation to O.
- (3) For each site j, let d(j) be the distance between the jth row of O and the jth row of \tilde{O} .
- (4) Construct *O'* from *O* by taking a subset of the *t* rows with the lowest distances.
- (5) Run PCA on O', and return \hat{R} , an estimate of R given by the solution (the scores of the first k principal components).

Intuitively, d(j) is low when the k-rank approximation of O approximates the jth row of O well. Therefore, sites with a low value of d(j) are more likely to be DMRs, assuming the first k PCs correspond to cell type composition. Sites with high distances are more likely to be uncorrelated with the cell type composition,

and, therefore, removing them from the analysis results in a better correlation with the true cell type composition. The suggested approach captures the cell type composition better than both common methods used in deconvolution of RNA expression data and an alternative approach in which we select the top t most variable sites (**Supplementary Figs. 11** and **12**).

The algorithm will scale to any sample size achievable by a PCA implementation, as the running time is dominated by the calculation of the k top left singular vectors of O. The runtime of singular value decomposition is quadratic in the number of samples; however, more efficient methods such as the power method or sampling techniques 15,16 may result in considerably reduced runtime. Empirically, under a standard implementation of PCA, ReFACTor required no more than several minutes of execution time on all the data sets described here.

In principle, in the above procedure, one would want to use factor analysis instead of PCA, i.e., to assume that different sites have different values of σ_j . Factor analysis is performed in iterations, where in each iteration the values of each site are scaled. The first iteration of factor analysis is equivalent to PCA after standardization of each of the sites, which is the step taken in ReFACTor. Empirically, applying more iterations of the factor analysis did not improve the performance, and the value of σ_j was close to the value inferred in the first iteration (data not shown).

The ReFACTor components can be added as covariates to an EWAS. In the case of an inflated test statistic due to cell type composition, ReFACTor components can be added one by one until the desired decrease in inflation is achieved, similar to the approach suggested by Zou *et al.*².

Parameters selection. Throughout the analysis, we applied ReFACTor on the data with the top (t = 500) most informative methylation sites, consistent with a line of previous work that used subsets of 500-600 informative sites for capturing the cell type composition 1,3,6 . We set k = 6 to align with the number of cell types estimated in whole blood by the reference-based approach, and throughout the paper, unless mentioned otherwise, we used the first six ReFACTor components in the analysis of real data and the first five components in the analysis of simulated data (simulated with k = 5). The performance of ReFACTor was robust to a wide range of choices of t and to the choice of t (**Supplementary Figs. 13–16**).

Data sets and quality control. In order to evaluate the performance of ReFACTor, we used whole-genome methylation data from the GALA II data set⁷, a pediatric Latino population study. The study protocol was approved by the UCSF Human Research Protection Program, and IRB-approved informed consent was obtained from all participants before any study procedure was performed. Blood samples were collected from 573 participants and assayed on an Illumina 450K DNA methylation chip. Additional blood samples were collected for 95 of the samples four months later for obtaining cell counts. A complete blood count with automated white blood cell differential was performed by automated flow cytometry at CLIA certified laboratories (UCSF Medical Center, San Francisco, CA and Quest Diagnostics, Madison, NJ). Note that the results showing the correlation of ReFACTor to the cell counts (Fig. 1) demonstrate that methylation levels can predict cell type composition in the future, which is most likely

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NATURE METHODS

because cell type composition is stable over time. Out of the total 573 samples, 525 samples were available at the time of analysis (a subset of the individuals for whom genotypes were collected as well as part of the GALA II study). Samples with inconsistencies in the available identifiers conversion file (between genotypes and methylation data) were dropped. In addition, samples that demonstrated extreme values in the first two principal components on the methylation levels were removed (more than 2 s.d.). A total of 489 samples remained for the analysis (245 males and 244 females), and for 78 of them cell count measurements were available for five different cell types: lymphocytes, monocytes, and three granulocyte subtypes — neutrophils, eosinophils, and basophils. Probes from sex chromosomes were discarded, as well as consistently methylated probes and consistently unmethylated probes (mean value higher than 0.8 or lower than 0.2, respectively), as was previously suggested for EWAS8, resulting in 102,503 probes that were included in the analysis. The data were SWAN¹⁷ normalized and corrected for batch using COMBAT¹⁸. For the analysis, we estimated cell proportion levels of CD8T, CD4T, NK cells, B cells, monocytes and granulocyte cells, using an existing reference-based approach³. In order to compare between the cell proportion estimates and the available cell counts, we collapsed the four estimates of lymphocyte cell types (CD8T, CD4T, NK cells and B cells) into a single combined lymphocytes level. For both the COMBAT normalization and the estimation of cell proportions, we used the minfi package¹⁹. The GALA II methylation data are now publicly available in the Gene Expression Omnibus (GEO) database (accession number GSE77716).

We also measured the performance of ReFACTor on a data set that was first studied in a recent association study of DNA methylation with rheumatoid arthritis (RA), including 354 cases and 332 controls⁸ (193 males and 493 females). Blood samples were collected from the participants and assayed on an Illumina 450K DNA methylation chip. The data are publicly available and were downloaded from the GEO database (accession number GSE42861). We repeated the quality control procedure for the data applied in a recently published work² on the same data. We filtered out consistently methylated probes and consistently unmethylated probes (mean value higher than 0.8 or lower than 0.2, respectively), as previously suggested⁸, resulting in 103,638 probes that were included in the analysis. The probe values were corrected for age, sex, smoking, and batch using linear regression. For these data, we estimated cell proportion levels of T cells, NK cells, B cells, monocytes, and granulocyte cells, similarly to what was done for the GALA II data set.

ReFACTor's site selection. Informally, the sites selected by ReFACTor are chosen so that they are well-approximated by \tilde{O} , the low rank approximation of the original methylation matrix O. Put differently, in \tilde{O} the jth row corresponds to an approximation of the jth methylation site (the jth row of O). Since the low rank approximation uses the eigenvectors of OO^t , similarly to PCA, it maximizes the variance of the resulting low dimensional space defined by the k top eigenvectors. Thus, methylation sites that are highly variable across different cell types (or generally across different values of the main confounders) are expected to contribute substantially to the low rank approximation, and they will therefore be well-approximated by the ReFACTor procedure. For a comparison between the feature selection and algorithmic

details underlying ReFACTor and those of other methods see **Supplementary Table 4**.

We found 90 methylation sites in the intersection of the 500 sites determined as the most informative by ReFACTor on the GALA II data, and the list of top DMRs previously reported in leukocyte cells¹ based on sorted leukocytes⁴ (P value < 10^{-50} , hypergeometric test). We also found 100 methylation sites in the intersection between the 500 sites determined to be the most informative by ReFACTor on the RA data, and the list of DMRs previously reported in leukocyte cells¹ based on sorted leukocytes⁴ (P value < 10^{-50} , hypergeometric test). Remarkably, we found most of the sites selected by ReFACTor for the RA data to be the same sites selected for the GALA II data (270 sites in the intersection; P value < 10^{-50} , hypergeometric test).

Data simulation. The methylation data were generated using a generative model in which a fraction p of the sites are DMRs; for each DMR we assume a normal distribution per cell type (with a potentially unique mean for each cell type). In non-DMR sites the mean methylation values of all cell types are equal. Each site was assumed to have a unique variance. The parameters of the model were set according to a methylation reference of sorted white blood cells (assayed on an Illumina 450K platform)⁴. The reference data are publicly available and were downloaded from the GEO database (accession number GSE35069). Since the reference includes only six individuals, we assume that the mean values of the cell types in DMRs are generated from a normal distribution with an s.d. of τ (shared across all DMRs). Thus, τ controls the level of cell composition information in DMRs. DNA methylation data were generated from a normal distribution (conditional on the range [0,1]) for five cell types per individual i and per site j, and cell type proportions were generated from a Dirichlet distribution. Finally, observed DNA methylation levels were composed for each individual by its simulated methylation levels and cell proportions. A random normal noise was added to every site to simulate technical noise (s.d. = 0.01).

DNA methylation levels were simulated for the same set of 103,638 sites used in the RA analysis, and the Dirichlet parameters were estimated from the cell type proportion estimates of the same data. Every simulated data set included 500 individuals. We estimated τ from the reference of sorted cells using maximum likelihood and found that τ = 0.07 fits the data best. The parameters of the normal distributions for generating the methylation levels were estimated from the reference as well. The proportion of DMRs was set to be p = 0.15, following a previous report in which the authors used the same reference of sorted cells in order to detect DMRs¹. Applying a Bonferroni correction for multiple hypotheses correction results in about 15% of the sites crossing the significance threshold.

We simulated three scenarios in order to evaluate the detection power of the methods. First, we generated continuous phenotypes using a linear model of the cell composition, a causal methylation effect, and a randomly distributed noise. The causal methylation site was randomly chosen along with one of the cell types that was used in the linear model. The effect size of the cell type was sampled from a standard normal distribution. We used several different levels for the effect size of the causal site. In the second set of simulations, the phenotypes were simulated by a linear model of the cell composition, the methylation levels of a

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randomly chosen site in a randomly chosen cell type (as opposed to total methylation level at the causal site), and random noise. Finally, in a third set of simulations we simulated ten causal sites; we simulated the phenotype as a linear function of a randomly chosen cell type, and then we randomly picked ten sites and added to their methylation levels a linear dependency in the phenotype, with varying effect sizes. In these simulations methylation levels were simulated only for the 10,686 sites from chromosome 1 that were available in the RA data. The restriction to a small number of sites was done to reduce runtime, as a few of the methods we assessed are computationally intensive and running hundreds of simulations becomes computationally prohibitive.

Estimating white blood cell proportions. Estimates were obtained using the default sites implemented in the minfi package¹⁹, defined and assembled for the 450K array¹ based on the approach described by Houseman *et al.*³ and 450K reference data⁴.

FaST-LMM-EWASher and RefFreeEWAS. We executed FaST-LMM-EWASher² and Ref-FreeEWAS⁵ using the default

parameters. For the latter, we used 250 bootstraps in each execution and applied the methodology proposed by the authors for determining the dimension parameter d (determined d = 46 for the GALA II data set and d = 43 for the RA data set).

Code availability. Python and R software associated with our method is available online (http://www.cs.tau.ac.il/~heran/cozygene/software/refactor.html) and is accompanied by a complete set of documentation and instructions. Additional tools for guiding the parameters selection for the ReFACTor algorithm are provided as well.

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