



Group Fairness by Probabilistic Modeling with Latent Fair Decisions

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Why algorithmic fairness

Al systems are increasingly being adopted in areas with personal and societal impact.

Societal bias may be perpetuated and amplified by AI/ML models





for a seri

Google apologises for Photos app's racist blunder





Challenge #2: Fairness guarantees hold only if the real-world distribution is captured.



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$$\mathbb{E}_{P_{data}}[f|S=1] - \mathbb{E}_{P_{data}}[f|S=0] = 0.13$$

f does not satisfy demographic parity!

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f is considered fair with respect to *Q*

Challenge #2: Fairness guarantees hold only if the real-world distribution is captured.

Our contribution: address both challenges using *probabilistic modeling* with *latent fair decisions*

Spoiler alert





Results: closely modeling the observed data distribution and bias mechanism leads to competitive *classification accuracy* and better *fairness guarantees*.



Sensitive attribute *S*, set of features *X*, label *D*





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Latent variable D_f to represent the hidden, fair label.



Assumption #1: D_f satisfies demographic parity. $\mathbb{E}_P[f(\mathbf{X}, S) | S = 1] = \mathbb{E}_P[f(\mathbf{X}, S) | S = 0]$



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 $\Rightarrow D_f \perp S$ for probabilistic classifier $f(\mathbf{X}, S) = P(D_f | \mathbf{X}, S)$





S,X,D	P(S,X,D)
1,1,1	0.2
1,1,0	0.1
:	:
0,0,0	0.3



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:	:
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S,X,D	$P(S,X,D,D_f=1)$	P(S,X,D,D _f =0)
1,1,1	0.15	0.05
1,1,0	0.05	0.05
:	:	÷
0,0,0	0.1	0.2



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:	:	:
0,0,0	0.3	0



Assumption #2: data provides information about D_f

 $\Rightarrow D \perp X \mid D_f, S$ to model dependence to D_f

S,X,D	P(S,X,D)
1,1,1	0.2
1,1,0	0.1
:	:
0,0,0	0.3

$P(S,X,D,D_f=1)$	P(S,X,D,D _f =0)
0.15	0.05
0.05	0.05
÷	÷
0.1	0.2
	<i>P(S,X,D,D_f=1)</i> 0.15 0.05 ⋮ 0.1

S,X,D	P(S,X,D,D _f =1)	P(S,X,D,D _f =0)
1,1,1	0.2	0
1,1,0	0.1	0
:	÷	:
0,0,0	0.3	0



Learn the distribution that best fits the data while ensuring $D_f \perp S$ and $D \perp X \mid D_f, S$.

Probabilistic circuits

Recursively define distributions using *sums*, *products*, and *univariate distributions*.

$$\Pr_{n}(\mathbf{x}) = \begin{cases} f_{n}(\mathbf{x}) & \text{if } n \text{ is a leaf} \\ \prod_{c \in \mathsf{ch}(n)} \Pr_{c}(\mathbf{x}) & \text{if } n \text{ is a product} \\ \sum_{c \in \mathsf{ch}(n)} \theta_{n,c} \Pr_{c}(\mathbf{x}) & \text{if } n \text{ is a sum} \end{cases}$$

- Expressive: closely model the data
- Tractable: efficiently compute conditionals
- Structure encodes independencies



 $P(D, X, D_f = 1, S = 1)$

Parameters are conditional probabilities $\theta_1 = P(D_f = 1, S = 1)$

Structure encodes conditional independence $P(D, X | D_f, S) = P(D | D_f, S) \cdot P(X | D_f, S)$



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- Learn the structure for *X* from data.
- Learn the parameters via EM:

$$\theta_{n,c}^{(\text{new})} = \operatorname{EF}_{\mathcal{D},\theta}(n,c) / \sum_{c \in \mathsf{ch}(n)} \operatorname{EF}_{\mathcal{D},\theta}(n,c).$$



Experiments: modeling the data



Experiments: similarity to observed labels



Experiments: synthetic data





- 1. Latent variable approach can learn *fair decisions* while explaining the data with *biased labels*.
- 2. Closely modeling the data leads to *lower discrimination scores*.
- 3. Latent decision variables from FairPC retain *high similarity* to observed *labels.*