CS247: ADVANCED DATA MINING

06Text Data: Word Embedding

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Announcement

- Midterm Exam
  - In class May 7th
  - Closed-Book Exam, no cell phone
  - Bring a simple electronic calculator
  - You can bring an A4 size reference sheet

Methods to Learn

	Vector Data	Text Data	Graph & Network	Recommender Systems
Classification	**Naïve Bayes; Logistic Regression; NN**		Label Propagation	
Clustering	**K-means; kernel k-means; Mixture Models**	**PLSA; LDA**	Spectral Clustering	Matrix Factorization
Prediction	**NN**			Collaborative Filtering; Factorization machine; Hybrid CF; Recommendation with graph regularization
Ranking			PageRank	
Similarity Search			P-PageRank	
Representation Learning		**Word embedding**	Network embedding	Deep collaborative learning

Text Data: Word Embedding

- Introduction to Word Representation
- Word2vec: CBOW and Skip-Gram
- GloVe: Global Vectors for Word Representation
- Summary

Why Word Representation?

- Finding Synonyms: words that have the same meaning
  - E.g., movie and film
- Finding polysemy: words with multiple meanings
  - E.g., light
- Document representation
  - E.g., aggregation of all the word representation

How to Represent a Word?

- Challenge
  - Discrete structure
- Simple representation
  - One-hot representation: a vector with one 1 and a lot of zeroes
  - E.g., Motel =

[0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0]

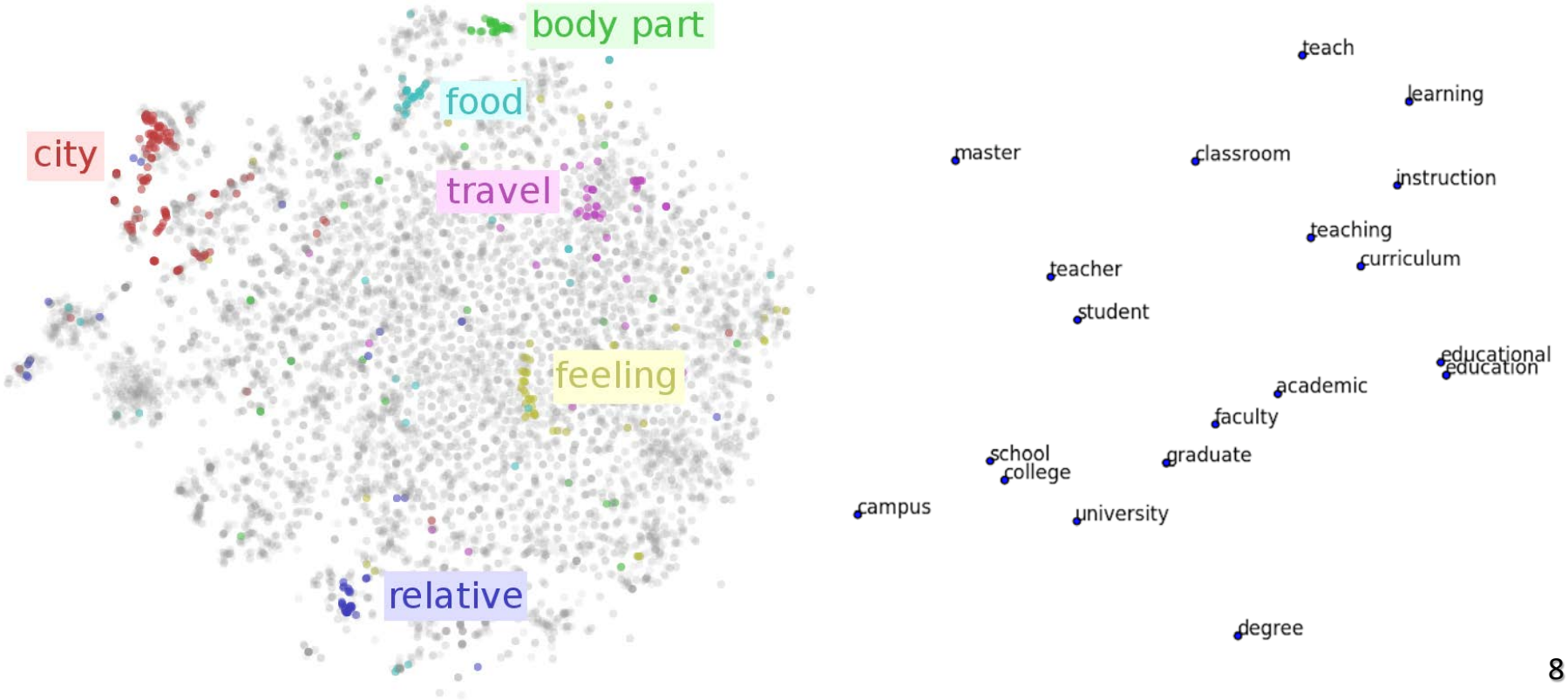
Problem of One-Hot Representation

- High dimensionality
  - E.g., for Google news, 13M words
- Sparse
  - Only 1 non-zero value
- Shallow representation
  - E.g.,

motel [0 0 0 0 0 0 0 0 0 0 1 0 0 0 0] AND
hotel [0 0 0 0 0 0 0 1 0 0 0 0 0 0 0] = 0

Word Embedding

- Low dimensional vector representation of every word
  - E.g., motel = [1.3, -1.4] and hotel = [1.2, -1.5]



How to Learn Such Embeddings?

- Using context information!

...he curtains open and the moon shining in on the barely...

...ars and the cold , close moon " . And neither of the w...

...rough the night with the moon shining so brightly , it...

...made in the light of the moon . It all boils down , wr...

...surely under a crescent moon , thrilled by ice-white...

...sun , the seasons of the moon ? Home , alone , Jay pla...

...m is dazzling snow , the moon has risen full and cold...

...un and the temple of the moon , driving out of the hug...

...in the dark and now the moon rises , full and amber a...

...bird on the shape of the moon over the trees in front...

A Naïve Approach

- Build a co-occurrence matrix for words, and apply SVD
  - Example Corpus:
    - I like deep learning.
    - I like NLP.
    - I enjoy flying.
- Issues:
  - Global context
  - SVD is very expensive

counts	I	like	enjoy	deep	learning	NLP	flying	.
I	0	2	1	0	0	0	0	0
like	2	0	0	1	0	1	0	0
enjoy	1	0	0	0	0	0	1	0
deep	0	1	0	0	1	0	0	0
learning	0	0	0	1	0	0	0	1
NLP	0	1	0	0	0	0	0	1
flying	0	0	1	0	0	0	0	1
.	0	0	0	0	1	1	1	0

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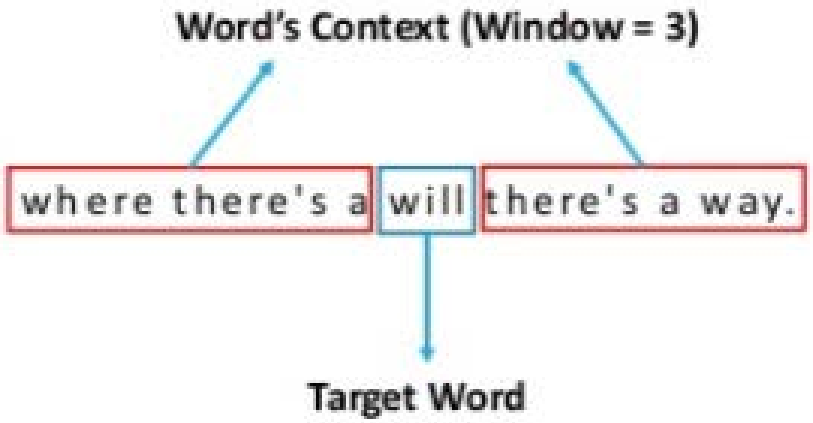
Word2Vec

- Proposed by Mikolov et al. at Google in 2013
- The most popular word embedding models
- Two architectures are proposed
  - Continuous bag-of-words (CBOW)
  - Skip-gram
- Extremely fast
  - "an optimized single-machine implementation can train on more than 100 billion words in one day"

Main Idea of Word2Vec

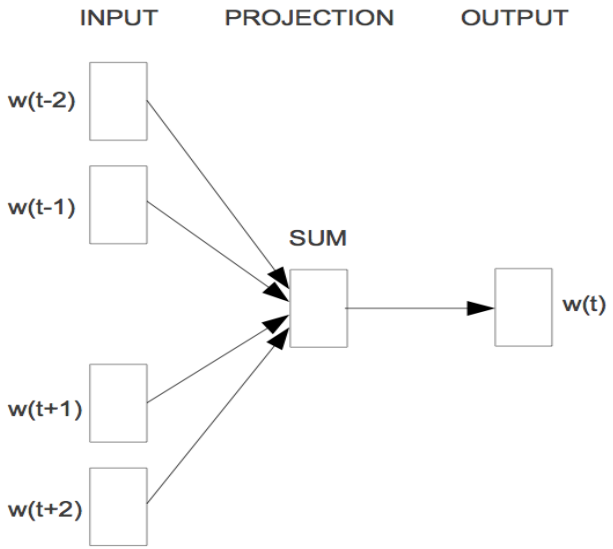
- Consider a local window of a target word



  - CBOW: predict the target words given the neighbors
  - Skip-gram: predict neighbors given the target words

CBOW

- Predicting target using neighbors

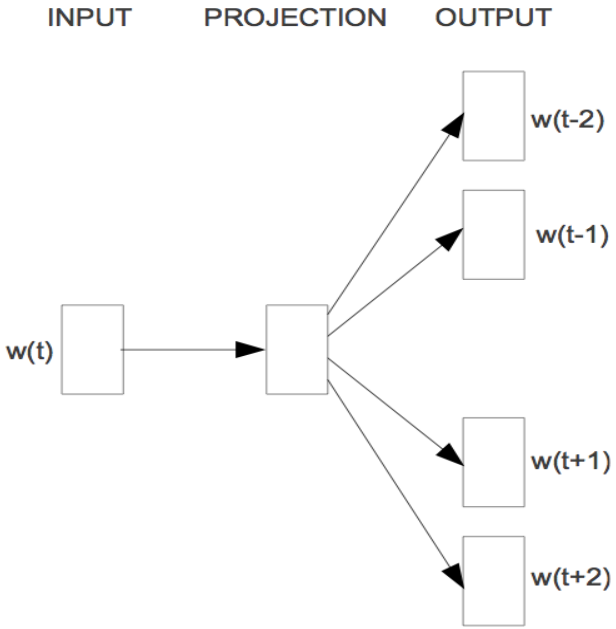


$$J_\theta = \frac{1}{T}\sum_{t=1}^{T} logp(w_t|w_{t-n},\dots,w_{t-1},w_{t+1},\dots,w_{t+n})$$

More details can be found in: http://www.1-4-5.net/~dmm/ml/how_does_word2vec_work.pdf

Skip-Gram

- Predicting neighbors using target



$$J_\theta = \frac{1}{T}\sum_{t=1}^{T}\sum_{-n\le j\le n, j\neq 0} logp(w_{t+j}|w_t)$$

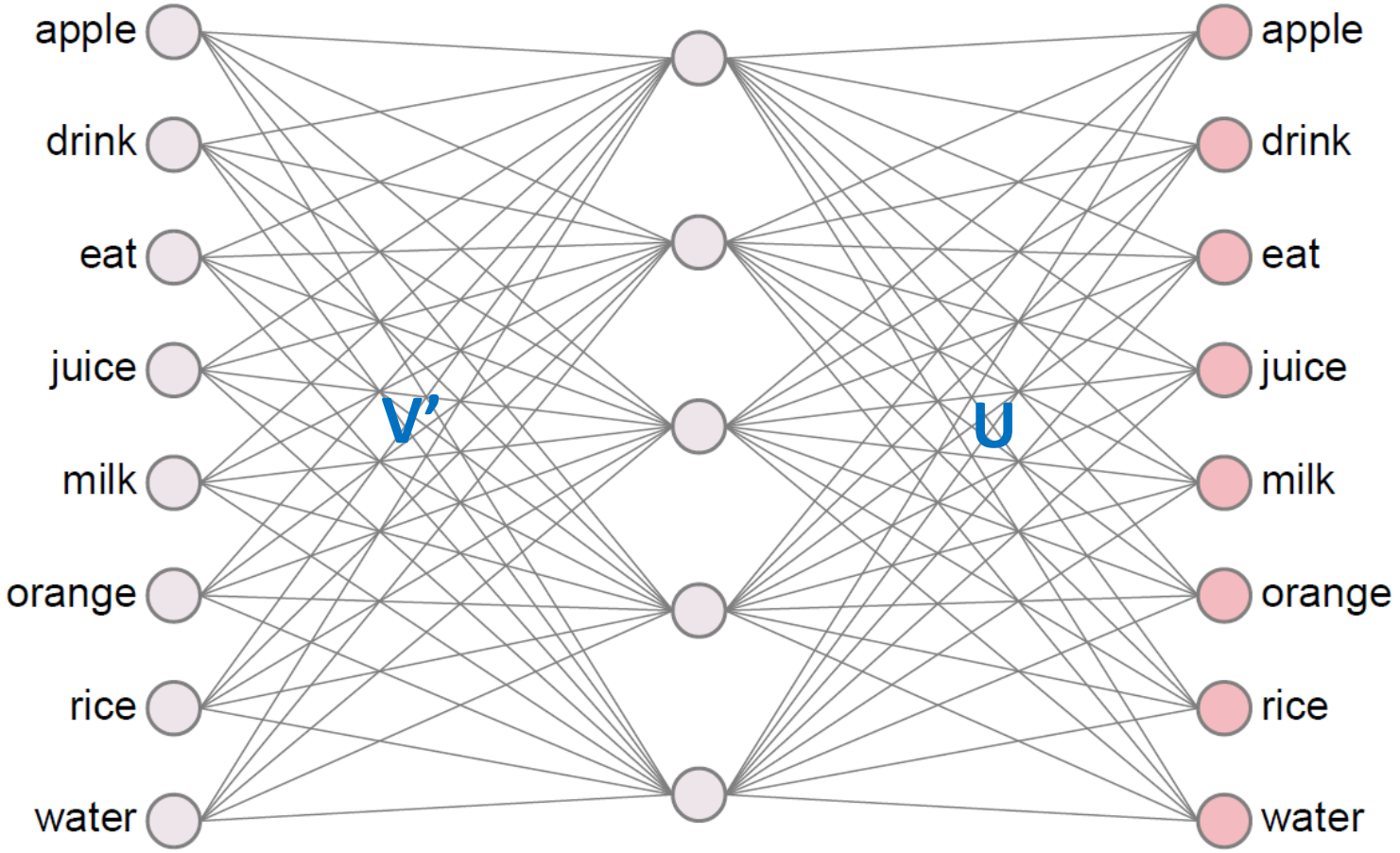
The Conditional Probability

- $p(w_{t+j}|w_t)$: the probability to see w_{t+j} in target word w_t's neighborhood
  - Intuition: w_t's embedding should be closer to w_{t+j}'s embedding
  - Every word has two embedding vectors
    - One serves as the role of target (***v***), and the other serves as the role of context (***u***)

$$p(o|w) = \frac{\exp(u_o^T v_w)}{\sum_{w'=1}^{N} \exp(u_{w'}^T v_w)}$$

(N is the total number of words in vocabulary)

A Neural Network Point of View



Input Layer:
one-hot vector

Hidden Layer:
Linear (Identity)

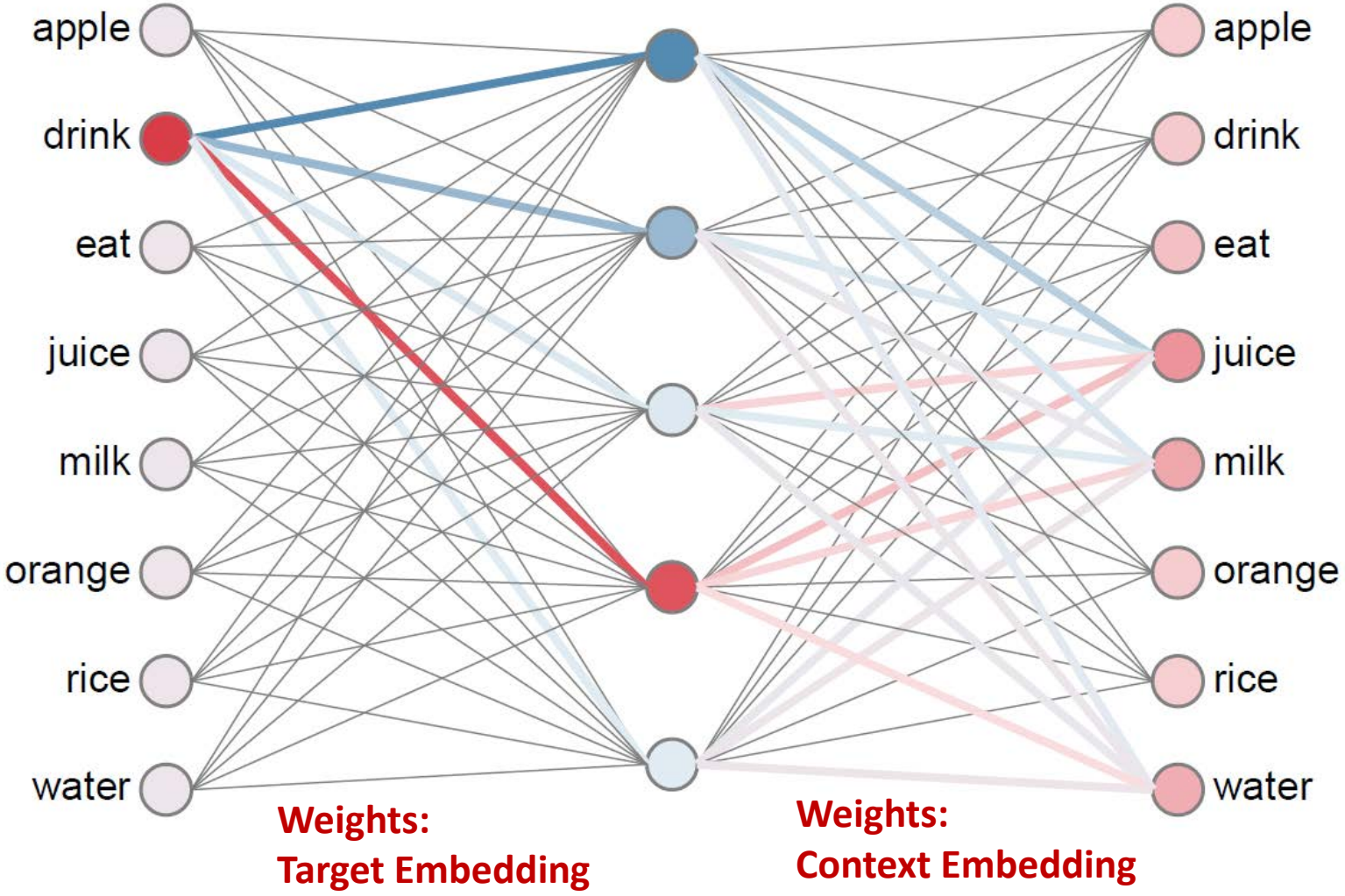
Output Layer:
softmax

Transformation Function under the Neural Network

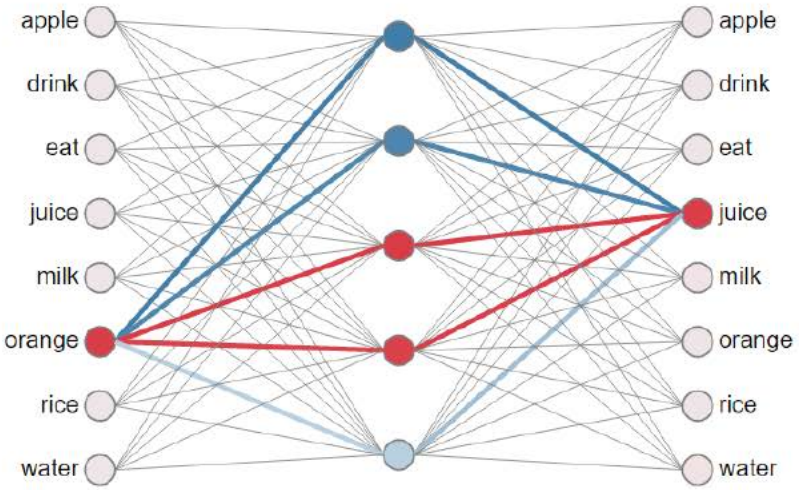
- Input: $\boldsymbol{x}$
  - One hot encoding vector
- Neural function: $y = f(\boldsymbol{x})$
  - $f(x) = softmax(UV^T\boldsymbol{x})$
    - $V: n \times d$
    - $U: n \times d$
- Output: $\boldsymbol{y}$
  - Probability vector indicating the probability to have each word in the vocabulary

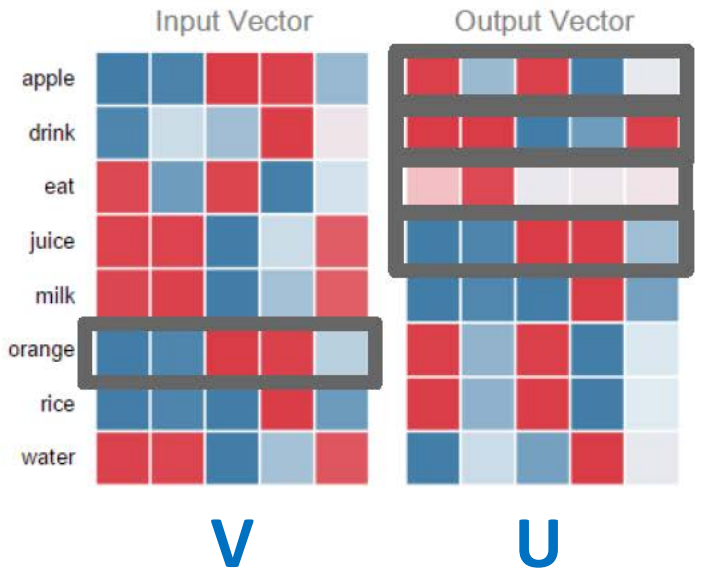
Demo

- https://ronxin.github.io/wevi/

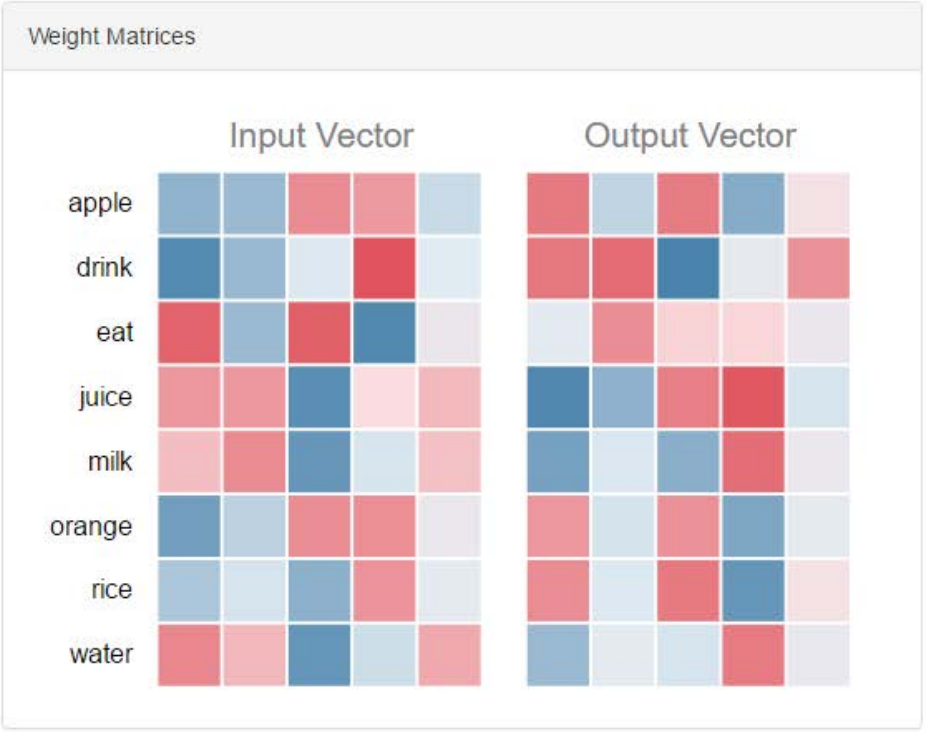


Embedding vs. NN Weights

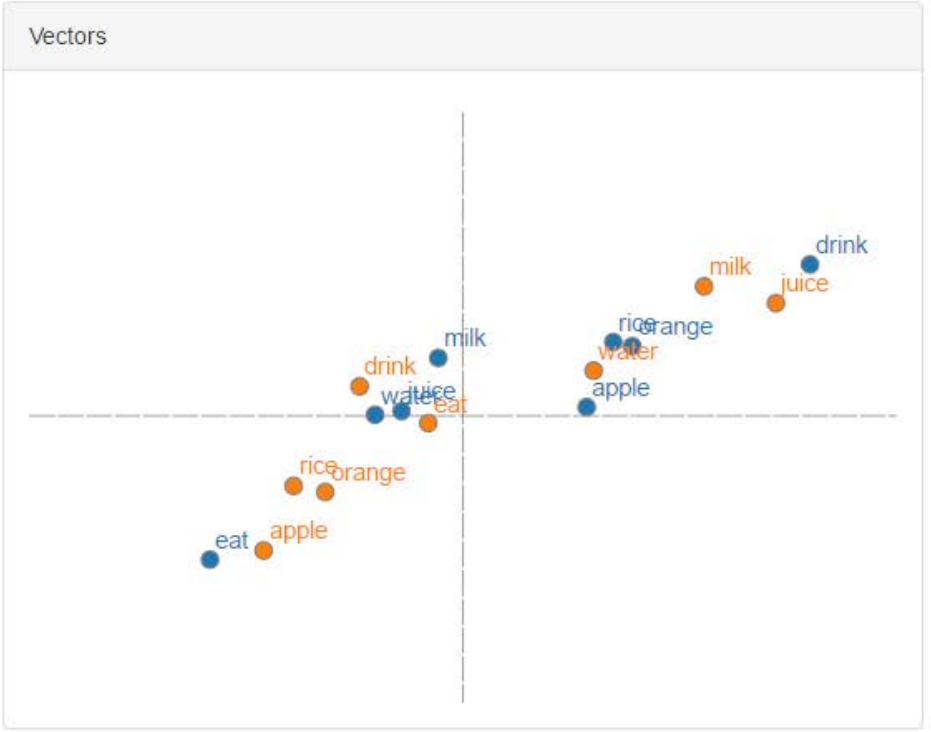




Embedding Visualization



V U



Original Objective Function

- The original objective is not scalable for large size vocabulary!

$$p(o|w) = \frac{\exp(u_o^T v_w)}{\sum_{w'=1}^{N} \exp(u_{w'}^T v_w)}$$

  - Maximize: $\prod_{(w,c)\in D} p(c|w)$
    - (w, c) denote any target word and context word pair

Negative Sampling for Skip-Gram

- For each target, for every positive word, sample k negative words

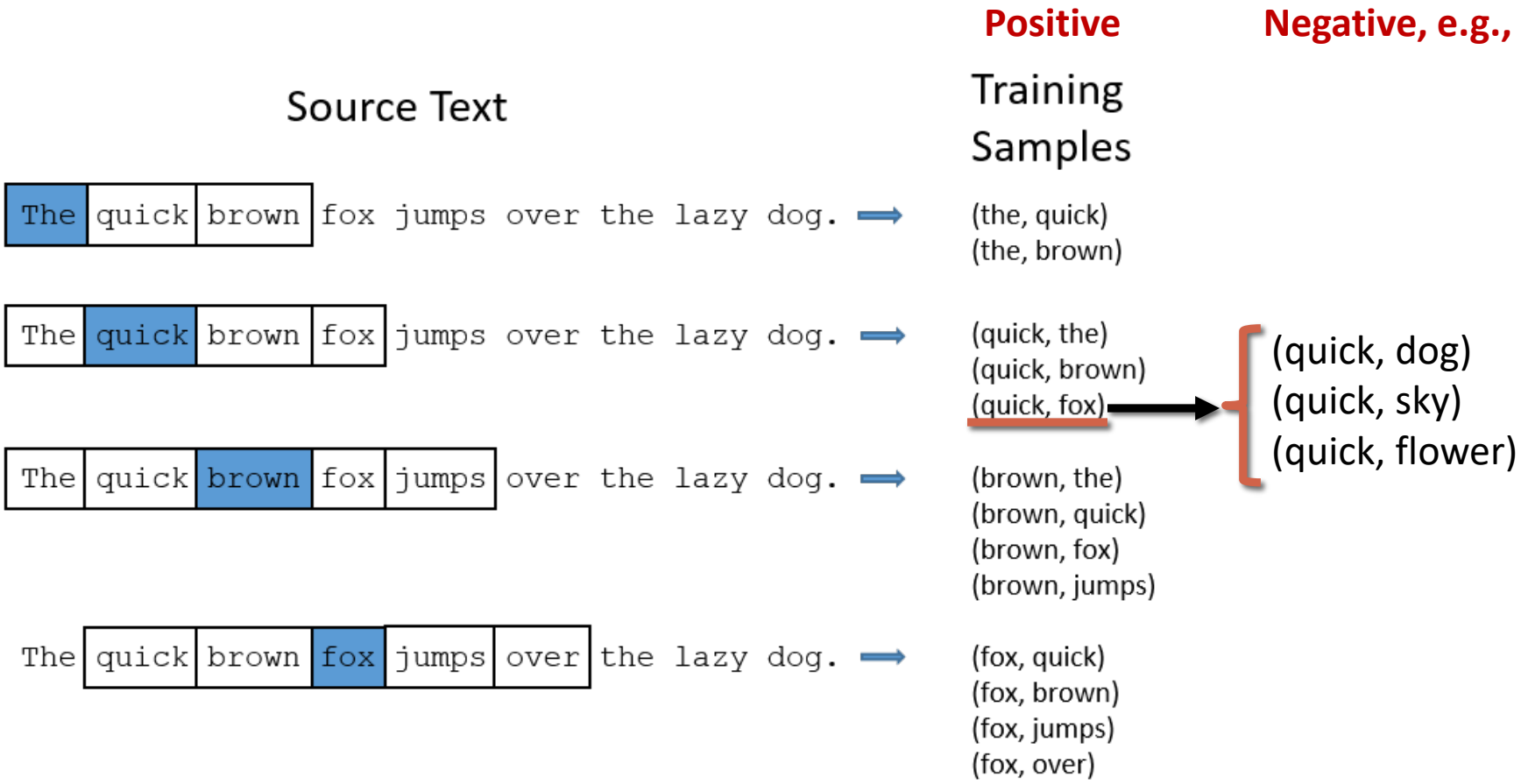
$$\sum_{(w,c)\in D}\left[log\sigma\left(u_c^{\mathrm{T}}v_w\right)+\sum_{i=1}^{k}E_{w_i\sim P_n(w)}[log\sigma(-u_{w_i}^{T}v_w)]\right]$$

$\boldsymbol{\sigma(\cdot)}$: **sigmoid function**

$P_n(w)$: **"Negative" Distribution**

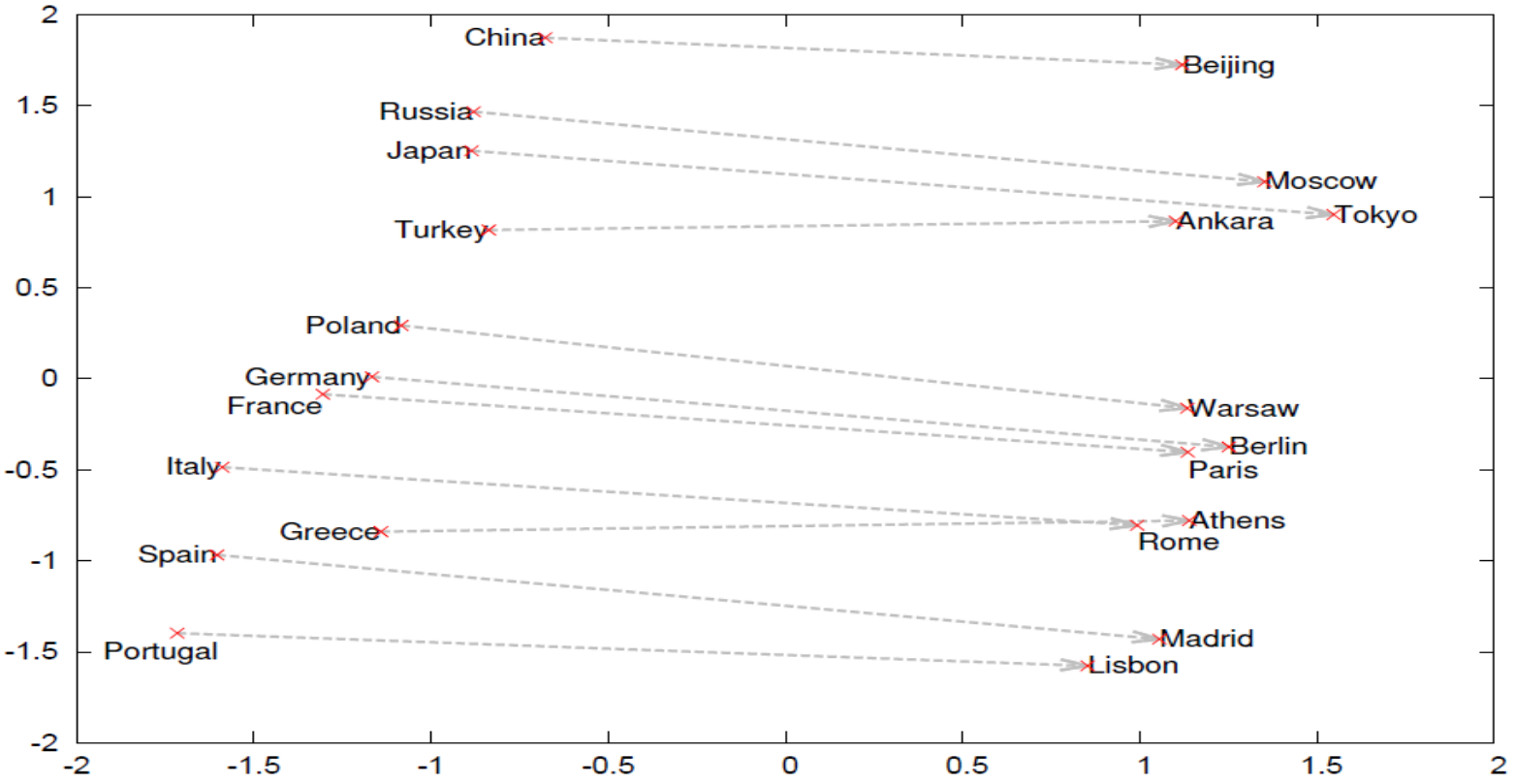
- **Examples: (1)** $\propto \boldsymbol{c(w)}$; **(2)** $\propto \left(\boldsymbol{c(w)}\right)^{\frac{3}{4}}$, $\boldsymbol{where\ c(w)}$ **is the total count of** w

More on Negative Samples



A Potential Application

- Relation detection and knowledge completion



$$v_{Germany} - v_{Berlin} \approx v_{France} - v_{Paris}$$

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Combining Two Worlds

- Matrix factorization for global word-word co-occurrence matrix
  - E.g., SVD
  - Global matrix factorization
- Make predictions within local context windows
  - E.g., word2vec
  - Local context window

Objective Function

Predicted value observed value

$$J = \sum_{i,j=1}^{V} f\left(X_{ij}\right)\left(w_i^T \tilde{w}_j + b_i + \tilde{b}_j - \log X_{ij}\right)^2$$

X_{ij}: number of times word j appears in the contex of word i

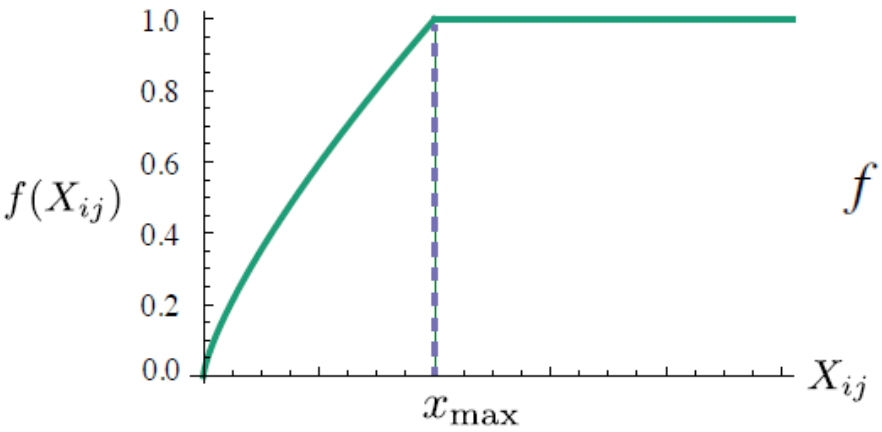
w_i: word vector for word i

$\tilde{w}_j$: context word vector for word j

b_i: bias term for word i

$\tilde{b}_j$: bias term for context word j

$f(X_{ij})$: a weighting function to punish high frequencies

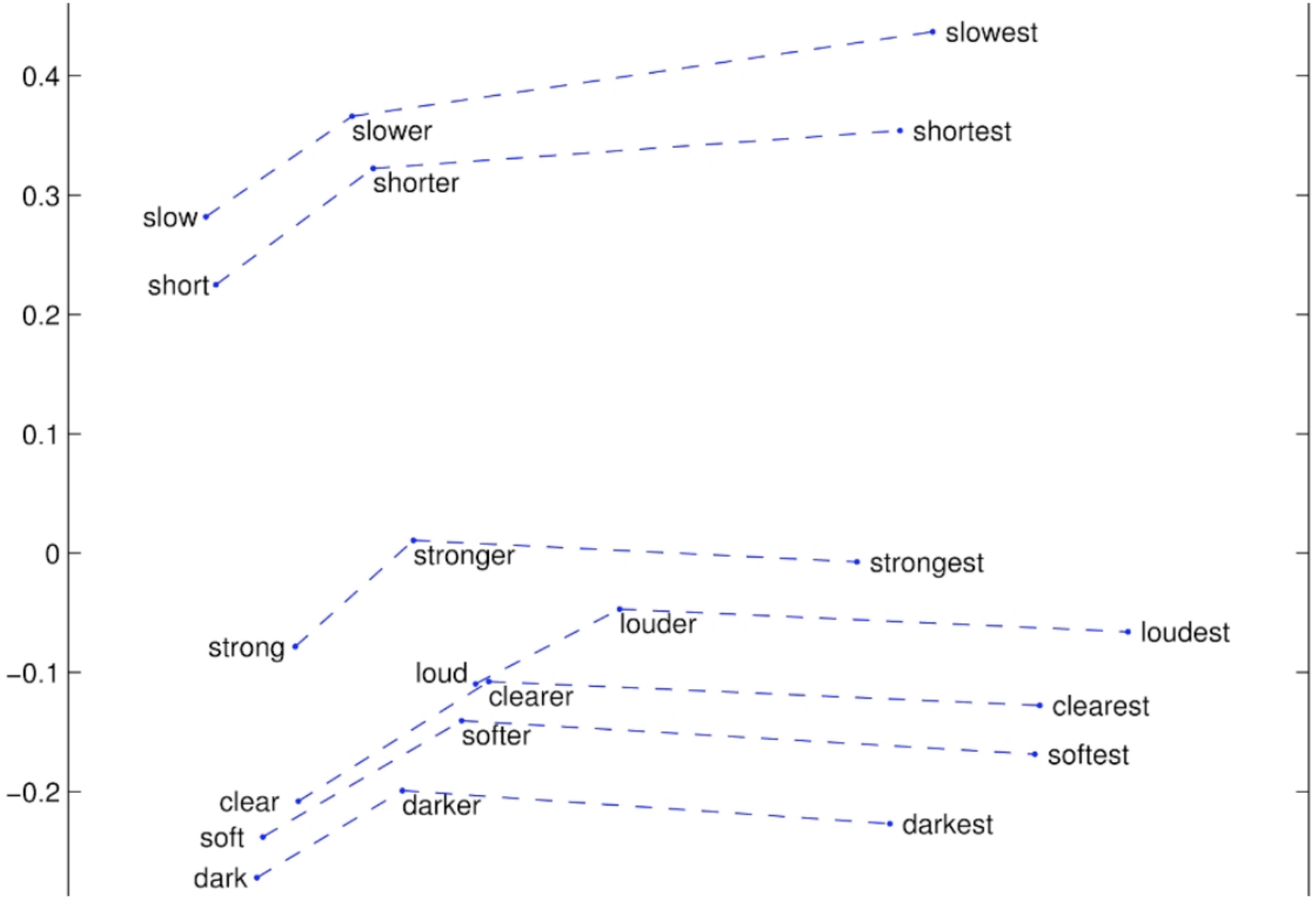


$$f(x) = \begin{cases} (x/x_{\max})^{\alpha} & \text{if } x < x_{\max} \\ 1 & \text{otherwise} \end{cases}.$$

Question

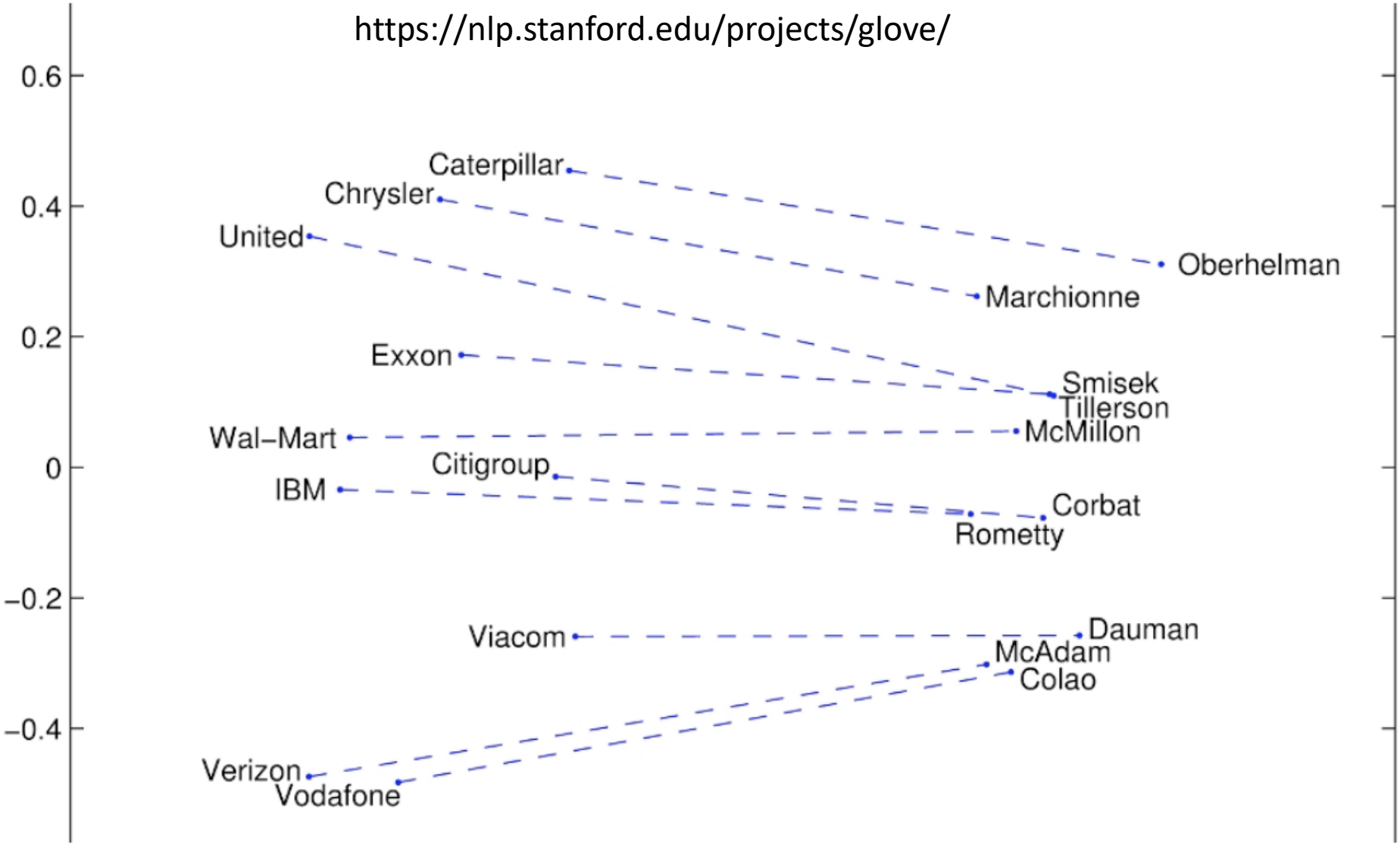
- How to optimize the objective function?

Some Interesting Results: Superlatives



Some Interesting Results: Company-CEO

https://nlp.stanford.edu/projects/glove/



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Summary

- Word embedding
  - A low-dimensional vector representation for words
- Word2vec
  - Local context-based prediction: CBOW and Skip-Gram
- Glove
  - Matrix decomposition on local context co-occurrence matrix

References

- Mikolov, T., Corrado, G., Chen, K., & Dean, J. (2013). Efficient Estimation of Word Representations in Vector Space. Proceedings of the International Conference on Learning Representations (ICLR 2013), 1–12.
- Mikolov, T., Chen, K., Corrado, G., & Dean, J. (2013). Distributed Representations of Words and Phrases and their Compositionality. NIPS, 1–9.
- Pennington, J., Socher, R., & Manning, C. D. (2014). Glove: Global Vectors for Word Representation. Proceedings of the 2014 Conference on Empirical Methods in Natural Language Processing, 1532–1543.
- Yoav Goldberg and Omer Levy (2014). Word2vec Explained: Deriving Mikolov et al.'s Negative-Sampling Word-Embedding Method. https://arxiv.org/pdf/1402.3722v1.pdf