QDiff: Differential Testing of Quantum Software Stacks

Jiyuan Wang, Qian Zhang, Harry Xu, and Miryung Kim

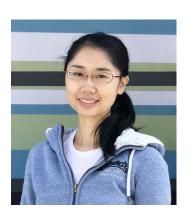
University of California, Los Angeles



TEAM MEMBERS



Jiyuan Wang



Qian Zhang



Harry Xu



Miryung Kim

People are using hardware accelerators







FPGA GPU Quantum Computer

Quantum Computers (QCs) are promisinghardware accelerators





Classical: O(2ⁿ)







Classical: O(e^{P(logN)})





Quantum: $O(2^{\sqrt{n}})$







Quantum: O(P(logN))

Grover algorithm can speed up unstructured search with a quantum computer.

Shor algorithm can speed up integer factorization with a quantum computer.

Quantum platforms are becoming publicly available













A study of real world errors in Qiskit, Cirq, and Pyquil

- We studied 76 bugs posted on StackOverflow and Github regarding Qiksit, Cirq, and Pyquil.
- Errors happen in three parts: language constructs, compilers, and simulators, which we call quantum software stacks (QSS).

Survey Statistics				
Keywords Searched	Quantum framework bugs, error, unexpected behavior			
Posts Studied in total	76 posts			
Common Fault Types	4			

Error Types	Percentage	Example
Bugs in Language Constructs	11.8%	Qiskit crashes on cnot() gate
Bugs in Compiler Setting	53.9%	Qiskit has bugs at the compiler optimization level
Bugs in Different Simulators	19.7%	Pyquil crashes on PyQvm with controlled gates
Bugs in Installation / Interaction with Other Tools	14.6%	Qiskit installation fails with Python 3.9

Errors in QSS are hard to identify

Challenge 1: Inherent probabilistic nature of quantum computing makes the error detection hard.

Challenge 2: There are very few quantum programs out here.

Challenge 3: Wait time is long due to limited public access to expensive quantum hardware.

QDiff's solutions

Challenge 1: Inherent probabilistic nature of quantum computing makes the error detection hard.



Differential test with Kolmogorov-Smirnov (KS) test [1] based distribution comparison.

Challenge 2: There are very few quantum programs out here.



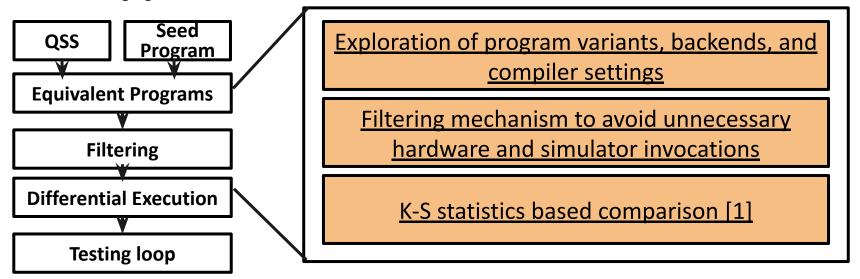
Generate more quantum programs with equivalent transformations.

Challenge 3: Wait time is long due to limited public access to expensive quantum hardware.



Avoid unnecessary invocations of a quantum simulator and hardware with static characteristics of quantum circuits.

QDiff approach overview



We found 4 software crashes in the **Cirq** and **Pyquil** simulations, and 2 possible root causes of 29 divergence cases on **IBM** quantum hardware.

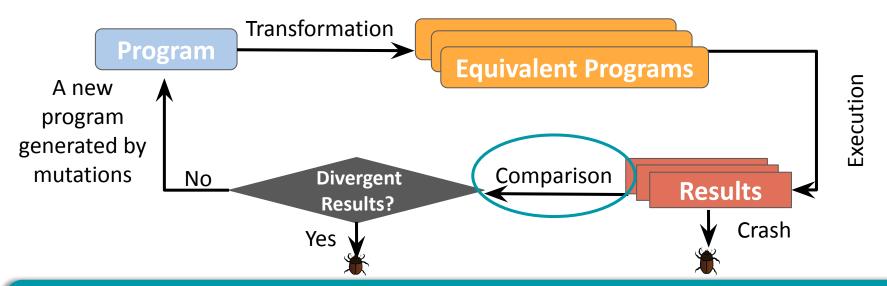
Approach 1: Equivalent program transformation

- QDiff transforms gates across their equivalent forms
 - We pick 7 commonly used rules in quantum compilation [2] and users can easily extend their own rules.
- QDiff also varies backend settings and compiler optimizations.

Rule ID	Original Gate	Equivalent Gate
G1	SWAP(p,q)	CNOT(p,q)CNOT(q,p)CNOT(p,q)
G2	S(p)	T(p)T(p)
G3	X(p)	H(p)S(p)S(p)H(p)
G4	Z(p)	S(p)S(p)
G5	CZ(p,q)	H(q)CX(p,q)H(q)
G6	CZ(p,q)CZ(p,q)	merged to Identity Matrix
G7	CCNOT(p,q)	6 CNOT gates with 9 one-qubit gates

^{2.} K. Hietala, R. Rand, S.-H. Hung, X. Wu, and M. Hicks, "A verified optimizer for quantum circuits," Proceedings of the ACM on Programming Languages, vol. 5, no. POPL, pp. 1–29, 2021.

Approach 2: Differential testing with distribution comparison



QDiff uses K-S test [1] to compare the distributions. We report the divergence if the K-S statistic is larger than a threshold.

Approach 2: KS based comparison

- Cumulative Probability with respect to the total trial number N.
- **K-S Statistic** is the max distance **D** between two measurement results.
- QDiff checks if **D** > a user-defined threshold **t**.
- The total trial number N can be determined by t and the confidence level p, which are given by users [3].

Measurement Distribution	'00'	'01'	'10'	'11'
N1	250	250	250	250
N2	247	247	253	253

Cumulative Probability	'00'	'01'	'10'	'11'
S1	0.250	0.500	0.750	1.00
S2	0.247	0.494	0.747	1.00

Approach 3: Filtering mechanism

- In the quantum theory, a qubit can retain a correct state for only a limited amount of time, called T1 time.
- 2-qubit gate dominates the error rate of the circuit.

Filtering mechanism: execution_time < T1 & #(2qgate) < th



Quantum circuits

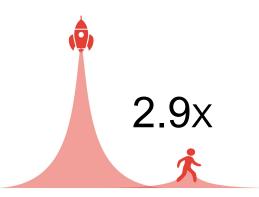
Analyzing the number of 2-qubit gates, a circuit depth and execution time

Executing on quantum hardware

Evaluation: Generation, speed up, and divergence



We generated 730 different quantum programs with semantic modifying mutations. The programs in turn produced 14799 circuits with equivalent transformations.



We reduced 66% unnecessary quantum hardware and simulator invocations.



We found 4 crashes in the quantum simulators and 2 root causes of 29 divergences with the quantum hardware.

Differential testing on quantum simulators

4 crashes we found in quantum simulators and they have been confirmed with QSS developers.

```
qvm = get_qc('3q-qvm')
try:
    qvm.run(Program())
except:
    print("empty")
.....
qvm.run(Program(H(1)))
```



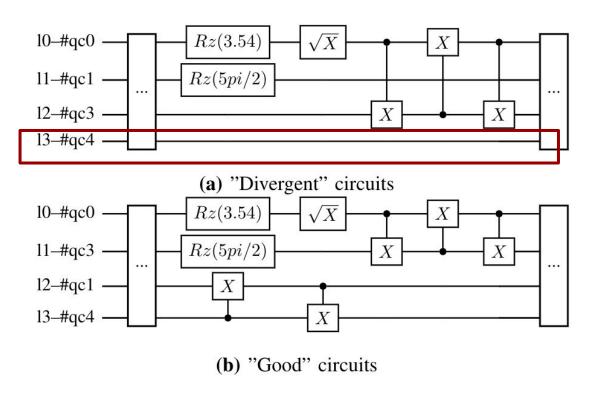
Example: Pyquil's simulator is stuck after executing an empty circuit https://github.com/rigetti/pyquil/issues/1034.

Differential testing on IBM quantum hardware

- We found 29 divergence cases in hardware executions:
 - These divergence cases might due to quantum circuit synthesis or compilation.
 - Equivalent programs produce measurements that are flagged as divergence in terms of K-S statistics.
- We speculated 2 possible root causes for 25 of them:
 - qubit dephasing [4]: 9 cases.
 - 2-qubit gate mapping [5]: 16 cases.

^{4. &}lt;a href="https://quantumai.google/cirq/google/best_practiceskeep_qubits_busy,2021">https://quantumai.google/cirq/google/best_practiceskeep_qubits_busy,2021

Differential testing on IBM quantum hardware





Qubit dephasing: no operation on #qc4 for too long time [4].

^{4.} https://quantumai.google/cirq/google/best_practiceskeep_qubits_busy,2021

QDiff: Differential Testing of Quantum Software Stacks

- •We are the first one to adapt differential testing to quantum software stacks.
- QDiff is effective in
 - generating quantum program variants;
 - avoiding unnecessary invocations of the quantum simulator and hardware;
 - We need deeper hardware knowledge to understand the root causes of our findings.
 - We need further effort to isolate software stack errors from hardware noises.
 - QDiff on Github: https://github.com/UCLA-SEAL/QDiff

Thanks for listening! O&A